**Registration Number:** 

Date & session:

## ST. JOSEPH'S UNIVERSITY, BENGALURU -27 M.Sc. (STATISTICS) – I SEMESTER SEMESTER EXAMINATION: OCTOBER 2022 (Examination conducted in December 2022) ST 7421 – Mathematical Analysis and Linear Algebra

Time: 2 Hours

Max Marks: 50

This paper contains <u>TWO printed pages and ONE part</u>

## PART-A

## Answer <u>FIVE FULL</u> Questions

- A) Define (i) Interior point of a set (ii) Limit point of a set with an example each.
   B) Define Metric Space. Show that the following are metric spaces. Show that d(x, y)=|x-y| is a metric for x, y ∈ R.
- 2. A) Define point-wise Continuity and Uniform Continuity of a function.B) Prove that any function continuous in closed interval is uniformly continuous. (3+7)
- 3. A) State and prove Cauchy's general principal of convergence of sequence..
  - B) Prove that absolute Convergence of a series of arbitrary terms implies its convergence. (5+5)
- 4. A) Examine for uniform convergence of  $f_n(x) = x/n, 0 \le x \le \alpha < \infty$ .
  - B) State and Prove Cauchy's criterion for uniform convergence of sequence of functions. (4+6)
- 5. A) Define Radius of convergence of power series. Obtain radius of convergence of  $\sum_{n=0}^{\infty} x^n/n^2$ .

B) if  $\int_a^b f_1(x) dg(x)$  and  $\int_a^b f_2(x) dg(x)$  exists then prove that

$$\int_{a}^{b} (f_{1}(x) + f_{2}(x)) dg(x) = \int_{a}^{b} f_{1}(x) dg(x) + \int_{a}^{b} f_{2}(x) dg(x)$$
(4+6)

6. A) Evaluate the double integral  $\iint_{S} (2x^{3} + y^{3})d(x, y)$ ,  $S = \{(x, y): x \ge 0, x^{2} + y^{2} \le 1\}$ . B) State and prove completion theorem. (5+5)

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- 7. A) Define a basis of a vector space and subspace of a vector space and dimension of a vector space.
  - B) Find row echelon form of the matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 3 & 6 & 9 \end{bmatrix}$ . Hence find the rank A.
  - c) Define quadratic forms and different classifications of quadratic forms. (3+4+3)